

```
implicit double precision (a-h,o-z)
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
c      vdpdhl.in must be filled as follows:
c
c      .....
c
c      uses subroutines .....
c
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
dimension yt(514)
character filename*10
common/param1/a(256,256),yx(256),g(256),
f      rha(256),x(256),d(256),ipvt(256),gme,rinp,
f      epst,deltax,tref,n
double precision a,yx,g,rha,x,d,gme,rinp,
f      epst,deltax,tref
integer*4 ipvt,n
common/geomet/rl,b,rh,rho,rmseff,resme,stifme,as,amred,gm
double precision rl,b,rh,rho,rmseff,resme,stifme,as,amred,gm
common/ref/iwrite
open(10,iostat=ios,err=2000,file='vdpdhl.in',status='old')
read(10,99993)iwrite
print *,iwrite
read(10,99993)nd
print *,nd
read(10,99993)k
print *,k
read(10,99993)kwrite
print *,kwrite
read(10,99994)et
print *,et
read(10,99993)istept
print *,istept
read(10,99994)st
print *,st
read(10,99992)filename
print *,filename
open(9,iostat=ios,err=2000,file=filename,form='unformatted')
read(10,99992)filename
print *,filename
open(11,iostat=ios,err=2000,file=filename,form='unformatted')
read(10,99992)filename
print *,filename
open(12,iostat=ios,err=2000,file=filename,form='unformatted')
read(10,99992)filename
print *,filename
open(13,iostat=ios,err=2000,file=filename,form='unformatted')
read(10,99992)filename
print *,filename
open(14,iostat=ios,err=2000,file=filename,form='unformatted')
read(10,99992)filename
print *,filename
open(15,iostat=ios,err=2000,file=filename,form='unformatted')
read(10,99993)isw
print *,isw
read(10,99993)ifill
print *,ifill
read(10,99994)epst
print *,epst
read(10,99994)rl
print *,rl
read(10,99994)b
print *,b
read(10,99994)rh
print *,rh
read(10,99994)rho
print *,rho
read(10,99994)rmsme
print *,rmsme
read(10,99994)resme
print *,resme
read(10,99994)stifme
print *,stifme
read(10,99994)qm
```

```
print *,gm  
read(10,99994) am  
print *,am  
read(10,99994) as  
print *,as  
nr=nd/2  
  
c      read(11) adum,bdum,ndum,c dum,ddum,kdum  
c      read(12) adum,bdum,ndum,c dum,ddum,kdum  
c      read(14) adum,bdum,ndum,c dum,ddum,kdum  
c      read(15) adum,bdum,ndum,c dum,ddum,kdum  
c          kdum=1  
c      do 500 jcount=1,kdum  
c          read(11)(yt(j),j=2,nr)  
c          read(12)(yt(nr+j),j=2,nr)  
c          read(14) yt(1)  
c          read(15) yt(nr+1)  
c 500 continue  
rewind (11,iostat=ios,err=3000)  
rewind (12,iostat=ios,err=3000)  
rewind (14,iostat=ios,err=3000)  
rewind (15,iostat=ios,err=3000)  
do 1000 j=1,nd  
    yt(j)=0d0  
    if(j.le.nr-1) ipvt(j)=0  
1000 continue  
deltax=r1/dfloat(nr-1)  
t=st  
deltat=(et-st)/dfloat(k)  
amred=am/gm/as  
rmseff=2d0*rho*r1+rmsme  
call t3dlfm(nd,k,kwrite,deltat,istept,t,yt,isw,ifill)  
write(iwrite,99999) isw  
close(9)  
close(10)  
close(11)  
close(12)  
close(13)  
close(14)  
close(15)  
stop  
2000 write(iwrite,99996) ios  
stop  
3000 write(iwrite,99995) ios  
stop  
99999 format(' isw= ',i2)  
99996 format(' error in open statement, ios=',i5)  
99995 format(' error in rewind statement, ios=',i5)  
99994 format(d13.6)  
99993 format(i5)  
99992 format(a)  
end  
  
!  
!  
  
subroutine rhstl(t,yin,yout)  
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc  
c  
c      routine rhstl  
c  
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc  
c  
c      first version: october, 24th - november, 1st 1985  
c  
c      author: rob diependaal  
c  
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc  
c  
c      computes right hand side of differential equation  
c  
c      input parameters:  
c          t-time  
c          yin-dependent variable  
c  
c      output parameters:  
c          yout-right hand side
```

```
c      common parameters: param1 (see routine solid1)
c
c      uses subroutines
c
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
implicit double precision (a-h,o-z)
dimension yin(514),yout(514),ak(256,1)
common/param1/a(256,256),yx(256),g(256),
f    rha(256),x(256),d(256),ipvt(256),gme,rinp,
f    epst,deltax,tref,n
double precision a,yx,g,rha,x,d,gme,rinp,
f    epst,deltax,tref
integer*4 ipvt,n
common/geomet/rl,b,rh,rho,rmseff,resme,stifme,as,amred,gm
double precision rl,b,rh,rho,rmseff,resme,stifme,as,amred,gm
c    stiffn(xx,uu,vv)=2d4*dexp(-3d-1*xx)
stiffn(xx,uu,vv)=1d4*dexp(-3d-1*xx)
presed(tt)=3.16d-5*dsin(8d0*datan(1d0)*tt)
rmass(xx)=5d-1
c    beta(xx)=8d-2*dexp(5d-2*xx)
beta(xx)=1d0
c    b2(xx)=85d-2+3d-3*xx
b2(xx)=1d0
b1(xx)=b2(xx)-beta(xx)
pi=4d0*datan(1d0)
c
    if(t.eq.tref)goto 2000
    gme=resme*yin(n+1)+stifme*yin(1)
    g(1)=resist(0d0,yin(2),yin(n+2))*yin(n+2)+
f    stiffn(0d0,yin(2),yin(n+2))*yin(2)
    rinp=presed(t)
    if(t.le.4d0)rinp=rinp*dexp((4d0-t)*(t-4d0)/2d0)
    coef2=(gme-amred*rinp)
    yx(1)=(g(1)-coef2*rha(1))/d(1)
    do 1000 i=3,n
        g(i-1)=resist(x(i-1),yin(i),yin(n+i))*yin(n+i)+
f        stiffn(x(i-1),yin(i),yin(n+i))*yin(i)
        yx(i-1)=(g(i-1)-coef2*rha(i-1))/d(i-1)
1000 continue
    call dgesl(a,256,n-1,ipvt,yx,0)
2000 do 3000 i=2,n
        yout(i)=yin(n+i)
        yout(n+i)=yx(i-1)
3000 continue
    yout(1)=yin(n+1)
    sum=deltax*beta(0d0)*rl*yx(1)
    do 4000 j=2,n-1
        x1=x(j)
        sum=sum+2d0*deltax*beta(x1)*(rl-x1)*yx(j)
4000 continue
    yout(n+1)=(amred*rinp-gme-2d0*rho/pi/b/rh*sum)/rmseff
return
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
c
c      end of routine rhst1
c
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
end
subroutine t3dlfm(nd,k,kwrite,deltat,istept,t,yt,isw,ifill)
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
c
c      routine t3dlfm
c
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
c
c      first version: october 2nd, 1987
c
c      author: rob diependaal
c
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
c
c      computes displacement, velocity, and pressure
c      in the time domain, based on a 3d-model with two boundary
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c      conditions in the place.  
c      writes the computed quantities to background memory  
  
c      input parameters:  
c          nd:    dimension of yt  
c          k:     number of time steps  
c          kwrite: time step from which onwards the quantities  
c                  will be written to memory  
c          deltat: time step  
c          istept: =1 -integration step (in the time) is variable  
c                 =2 -integration step is constant  
c          t:     time  
c          yt:    contains displacement and velocity  
c          isw:   =1 -extra yx (see common) computations will be done  
c                =0 -no extra computations will be done  
c          ifill:=1 -a and x (see common) will be filled  
c                =0 -a must be filled and decomposed  
c                   and x must be filled  
  
c      output parameters:  
c          t,yt  
c          isw:   =0 -no error has occurred  
c                =2 -error in input parameters  
c                =3 -error in integration in the time  
  
c      common parameters:  
c          paraml: a,yx,g,x,epst,deltax,tref,n  
c                  a-matrix containing information about  
c                    discretisation in the place  
c                  yx-contains accelleration  
c                  g-contains pressure minus mass term  
c                  x-contains points along x-axis  
c                  epst-accuracy for integration in the time  
c                  deltax-place step  
c                  tref-reference time  
c                  n-number of discretisation intervals in the place  
  
c      uses subroutines  
  
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc  
implicit double precision (a-h,o-z)  
dimension yt(nd),yp(256),work(256)  
common/paraml/a(256,256),yx(256),g(256),  
f rha(256),x(256),d(256),ipvt(256),gme,rinp,  
f epst,deltax,tref,n  
double precision a,yx,g,rha,x,d,gme,rinp,  
f epst,deltax,tref  
integer*4 ipvt,n  
common/parlu/alu(256,3),blu(256,1),int(256),yxl(256)  
common/geomet/rl,b,rh,rho,rmseff,resme,stifme,as,amred,gm  
double precision rl,b,rh,rho,rmseff,resme,stifme,as,amred,gm  
common/ref/iwrite  
common/comsum/asi(1024),aco(1024),rnum(100,256),den(100,256)  
double precision asi,aco,rnum,den  
external rhstl  
stiffn(xx,uu,vv)=2d4*dexp(-3d-1*xx)  
stiffn(xx,uu,vv)=1d4*dexp(-3d-1*xx)  
! presed(tt)=3.16d-5*dsin(8d0*datan(1d0)*tt)  
presed(tt)=3.16d-7*dsin(8d0*datan(1d0)*tt)  
rmass(xx)=5d-1  
beta(xx)=8d-2*dexp(5d-2*xx)  
beta(xx)=1d0  
b2(xx)=85d-2+3d-3*xx  
b2(xx)=1d0  
b1(xx)=b2(xx)-beta(xx)  
dcoth(xx)=dcosh(xx)/dsinh(xx)  
epssum=1d-2  
epsmod=1d-4  
maxsum=1000  
maxmod=100  
pi=4d0*datan(1d0)  
alpha=8d0*rho/(pi*pi*b)*deltax  
pddh=pi*deltax/rh  
tpddh=2d0*pddh  
pdd2h=pddh/2d0
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      pdd4h=pdd2h/2d0
      t4=pi*r1/rh
      coef=8d0*rho/pi/rmseff
      grme=4d0*rho/rh/rmseff
c
c      tests
c
      if(nd.gt.514) isw=2
      if(isw.lt.0.or.isw.gt.1) isw=2
      if(k.le.0.or.k.lt.kwrite.or.kwrite.le.0) isw=2
      n=nd/2
      if(2*n.ne.nd) isw=2
      if(isw.eq.2) return
c
c      initiations
c
      if(ifill.eq.0) goto 2000
      do 1000 j=1,4*(n-1)
        asi(j)=dsin(dble(j)*pi/2d0/dble(n-1))
        aco(j)=dcos(dble(j)*pi/2d0/dble(n-1))
1000    continue
c
c      fills a, rha and x
c
      x(1)=0d0
      rha(1)=coef*r1
      aux=alpha*beta(0d0)
      x(2)=deltax
      x1=deltax
      t1=dlog(2d0*(dcosh(pddh)-1d0))
      t7=pdd2h*dcoth(pdd2h)
      t5=t7/2d0
      gr=t1-t4-t7-1d0
      do 1100 j=1,2
        bet=beta(dble(j-1)*deltax)
        bb1=b1(dble(j-1)*deltax)
        bb2=b2(dble(j-1)*deltax)
        do 1110 i=1,maxmod
          rnum(i,j)=dcos(dble(i)*pi*bb2/b)+
f              dcos(dble(i)*pi*bb1/b)
          help=dble(i)*bet/b
          den(i,j)=1d0-help*help
          if(dabs(den(i,j)).lt.1d-10) then
            den(i,j)=1d0
            rnum(i,j)=pi/2d0*dsin(pi*bb2/bet)
          endif
1110      continue
1100    continue
      next=idint(b/beta(0d0))
      nex1=next
      call sum3d(1,1,epssum,epsmod,gr,maxsum,maxmod,next,
f          deltax,n-1,gr3d)
      a(1,1)=aux*(gr/pi-gr3d+grme/2d0*r1*r1)-rmass(0d0)
      d(1)=dabs(a(1,1))
c      write(iwrite,*)a(1,1)
      rha(2)=coef*(r1-x1)
      t2=dlog(2d0*(dcosh(tpddh)-1d0))
      t6=pdd2h*dcoth(pddh)
      gr=t2-t4-t6-t7-5d-1
      next=max(nex1,idint(b/beta(x1)))
      call sum3d(2,1,epssum,epsmod,gr,maxsum,maxmod,next,
f          deltax,n-1,gr3d)
      a(2,1)=aux*(gr/pi-gr3d+grme/2d0*r1*(r1-x1))
      d(2)=dabs(a(2,1))
c      write(iwrite,*)a(2,1)
      a1=pddh
      do 100 i=3,n-1
        x1=x(i-1)+deltax
        x(i)=x1
        rha(i)=coef*(r1-x1)
        a1=a1+pddh
        t8=dlog(2d0*(dcosh(a1)-1d0))
        gr=t8-t4
        bet=beta(x1)

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      bb1=b1(x1)
      bb2=b2(x1)
      do 1120 ii=1,maxmod
        rnum(ii,i)=dcos(dble(ii)*pi*bb2/b)+
          f dcos(dble(ii)*pi*bb1/b)
        help=dble(ii)*bet/b
        den(ii,i)=1d0-help*help
        if(dabs(den(ii,i)).lt.1d-10) then
          den(ii,i)=1d0
          rnum(ii,i)=pi/2d0*dsin(pi*bb2/bet)
        endif
1120    continue
      next=max(nex1,idint(b/bet))
      call sum3d(i,1,epssum,epsmod,gr,maxsum,maxmod,next,
        f deltax,n-1,gr3d)
      a(i,1)=aux*(gr/pi-gr3d+grme/2d0*r1*(r1-x1))
      d(i)=dabs(a(i,1))
c      write(iwrite,*)a(i,1)
100    continue
      do 200 j=2,n-1
        x2=x(j)
        a4=pi*x2/rh
        aux=alpha*beta(x2)
        nex1=idint(b/beta(x2))
        do 210 i=1,n-1
          x1=x(i)
          a1=pi*x1/2d0/rh
          a2=2d0*a1
          a3=2d0*a2
          next=max(nex1,idint(b/beta(x1)))
          if(iabs(i-j).ge.2) then
            if(i.eq.1) then
              t1=2d0*dlog(2d0*(dcosh(a4)-1d0))
            else
              t1=2d0*dlog(2d0*dabs(dcoth(a2)-dcoth(a4)))
            endif
            gr=t1-2d0*t4
            call sum3d(i,j,epssum,epsmod,gr,maxsum,maxmod,next,
              f deltax,n-1,gr3d)
            a(i,j)=aux*(gr/pi-gr3d+grme*(r1-x1)*(r1-x2))
          else
            if(iabs(i-j).eq.1) then
              if(i.eq.1) then
                gr=2d0*(t1-t4)-t7-1d0
                call sum3d(i,j,epssum,epsmod,gr,maxsum,maxmod,
                  next,deltax,n-1,gr3d)
                a(i,j)=aux*(gr/pi-gr3d+grme*r1*(r1-x2))
              else
                t1=2d0*dlog(2d0*(dabs(dcoth(a2)-dcoth(a4))))
                t6=a1*dcoth(a2)
                if(i.lt.j) then
                  t3=2d0*x1/deltax*dlog(dsinh(a2+pdd2h)/dsinh(a2))
                  t8=(a1+pdd4h)*dcoth(a2+pdd2h)
                else
                  t3=2d0*x1/deltax*dlog(dsinh(a2)/dsinh(a2-pdd2h))
                  t8=(a1-pdd4h)*dcoth(a2-pdd2h)
                endif
                gr=t1+t3-t5-t6-t8-2d0*t4-5d-1
                call sum3d(i,j,epssum,epsmod,gr,maxsum,maxmod,
                  next,deltax,n-1,gr3d)
                a(i,j)=aux*(gr/pi-gr3d+grme*(r1-x1)*(r1-x2))
              endif
            else
              t1=dlog(4d0*(dcosh(pddh)-dcosh(a3))+2d0*
                f (dcosh(a3+pddh)+dcosh(a3-pddh)-
                f dcosh(tpddh)-1d0))
              t3=2d0*x1/deltax*dlog(dsinh(a2+pdd2h)/dsinh(a2-pdd2h))
              t6=a2*dcoth(a2)
              t8=(a1+pdd4h)*dcoth(a2+pdd2h)
              t9=(a1-pdd4h)*dcoth(a2-pdd2h)
              gr=t1+t3-t7-t6-t8-t9-2d0*t4-1d0
              call sum3d(i,j,epssum,epsmod,gr,maxsum,maxmod,
                next,deltax,n-1,gr3d)
              a(i,j)=aux*(gr/pi-gr3d+grme*(r1-x1)**2)-rmass(x1)
            endif
          endif
        do

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        endif
    endif
c      write(iwrite,*)a(i,j)
        d(i)=d(i)+dabs(a(i,j))
210    continue
200    continue
        print *, 'A is filled'
        write(9) n-1
        write(9) ((a(l1,l2), l1=1, n-1), l2=1, n-1)
        write(9) (rha(l1), l1=1, n-1)
        write(9) (x(l1), l1=1, n-1)
        write(9) (d(l1), l1=1, n-1)
c
c      equilibrates the rows of a
c
        do 300 i=1, n-1
            equil=d(i)
            do 310 j=1, n-1
                a(i,j)=a(i,j)/equil
c      write(iwrite,*)a(i,j)
310    continue
300    continue
c
c      decomposes a in lower and upper triangle
c
        call dgeco(a, 256, n-1, ipvt, rcond, work)
        write(9) ((a(l1,l2), l1=1, n-1), l2=1, n-1)
        write(9) (ipvt(l1), l1=1, n-1)
        rewind(9)
2000    if(ifill.eq.0) then
            read(9) nn
            read(9) ((a(l1,l2), l1=1, nn), l2=1, nn)
            read(9) (rha(l1), l1=1, nn)
            read(9) (x(l1), l1=1, nn)
            read(9) (d(l1), l1=1, nn)
            read(9) ((a(l1,l2), l1=1, nn), l2=1, nn)
            read(9) (ipvt(l1), l1=1, nn)
        endif
        ht=deltat
        tout=t
        k1=k+1
        jhelp=0
c
        do 3000 j=1, k1
c
c      do-loop over time variable
c
            write(iwrite, 33101) j
            format(' time step number: ', i7)
            if(isw.eq.0) goto 3300 !3200
            gme=resme*yt(n+1)+stifme*yt(1)
            g(1)=resist(0d0, yt(2), yt(n+2))*yt(n+2)+
f          stiffn(0d0, yt(2), yt(n+2))*yt(2)
            rinp=presed(t)
            if(t.le.4d0) rinp=rinp*dexp((4d0-t)*(t-4d0)/2d0)
            coef2=gme-amred*rinp
            yx(1)=(g(1)-coef2*rha(1))/d(1)
            do 3100 i=3, n
                i1=i-1
                xhelp=x(i1)
                g(i1)=resist(xhelp, yt(i), yt(n+i))*yt(n+i)+
f          stiffn(xhelp, yt(i), yt(nd+i))*yt(i)
                yx(i1)=(g(i1)-coef2*rha(i1))/d(i1)
3100    continue
            call dgesl(a, 256, n-1, ipvt, yx, 0)
            goto 3300
3200    isw=1
3300    jj=j-1
            jhelp=jhelp+1
            if(jj.lt.kwrite.and.jhelp.eq.128) then
                do 3310 kw=11, 12
                    write(kw) x(n-1), deltax, n-1, t, deltat, 1
                continue
! 3310
                do 3320 kw=14, 15

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      write(kw)0d0,0d0,1,t,deltat,1
!   3320         continue
!           write(11)(yt(1),l=2,n)
!           write(12)(yt(1),l=n+2,nd)
!           write(14)yt(1)
!           write(15)yt(n+1)
!           rewind (11,iostat=ios,err=5000)
!           rewind (12,iostat=ios,err=5000)
!           rewind (14,iostat=ios,err=5000)
!           rewind (15,iostat=ios,err=5000)
!           jhelp=0
!       endif
      if(jj.lt.kwrite)then
        goto 3600
      else if(jj.gt.kwrite)goto 3500
    else if(jj.eq.kwrite) then
      khelp=k1-kwrite
      tend=t+(khelk-1)*deltat
      do 3400 kw=11,13
        write(kw)x(n-1),deltax,n-1,tend,deltat,khelp
3400      continue
      do 3450 kw=14,15
        write(kw) 0d0,0d0,1,tend,deltat,khelp
3450      continue
    end if
c3500    do 3550 i=1,n-1
c          yp(i)=rmass(x(i))*yx(i)+g(i)
c3550    continue
3500    write(11)(yt(1),l=2,n)
      write(12)(yt(1),l=n+2,nd)
c          write(13)(yp(1),l=1,n-1)
c          write(14)yt(1)
c          write(15)yt(n+1)
3600    if(j.eq.k1)goto 4000
      iflag=istept
      tout=tout+deltat
      tref=t
3700    call rkf4st(rhst1,t,tout,yt,ht,nd,epst,iflag)
      if(iflag.eq.2)write(iwrite,33001)iflag
33001    format(' iflag=',i2)
      if(iflag.eq.2)goto 3700
      if(iflag.eq.3)goto 3000
      write(iwrite,99999)j
      isw=4
      return
3000  continue
4000  isw=0
      return
! 5000  write(iwrite,99995)ios
!       return
99999  format(' error in integration in t-direction, j= ',i5)
99995  format(' t3dlfm: error in rewind statement, ios=',i5)
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
c
c      end of routine t3dlfm
c
ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
end
double precision function resist(xx,u,vv)
implicit double precision (a-h,o-z)
c
if(dabs(vv).lt.1d-20)then
  r1=1d0
else
  r1=1d-4*dsinh(vv*1d4)/vv
endif
if(dabs(vv).gt.170d0)then
  r2=0d0
else
  r2=2d0/dcosh(vv*1d6)
endif
resist=25d-1*dsqrt(2d0)*(r1-r2)*dexp(-15d-2*xx)
c resist=5d0*dexp(-15d-2*xx)
return

```



```

      end
      subroutine sum3d(i,j,epssum,epsmod,gr,maxsum,maxmod,next,
f      deltax,ndim,gr3d)
cccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
c
c      routine sum3d
c
cccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
c
c      author: Rob Diependaal
c
c      first version: November 6th, 1987
c
cccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
      implicit double precision (a-h,o-z)
      common/comsum/asi(1024),aco(1024),rnum(100,256),den(100,256)
      double precision asi,aco,rnum,den
      common/geomet/rl,b,rh,rho,rmseff,resme,stifme,as,amred,gm
      double precision rl,b,rh,rho,rmseff,resme,stifme,as,amred,gm
      common/ref/iwrite
c
      pi=4d0*datan(1d0)
      m=4*ndim
      i1=i-1
      j1=j-1
      gr3d=0d0
      grref=gr*rl/pi
c
      do 1000 n=1,maxmod
         t1sq=dbl(n)*pi/b
         t1sq=t1sq*t1sq
         sum=0d0
         do 1100 k=0,maxsum
            coef=(dbl(k)+5d-1)*pi/rl
            coefsq=coef*coef
            gamma=dsqrt(coefsq+t1sq)
            if(j.eq.1) then
               if(i.ge.3) then
                  ind=mod((2*k+1)*i1,m)
                  term=aco(ind)
               else
                  if(i.eq.2) then
                     ind=mod(4*k+2,m)
                     term=asi(ind)/2d0/coef/deltax
                  else
                     ind=mod(2*k+1,m)
                     term=asi(ind)/coef/deltax
                  endif
               endif
            else
               if(iabs(i-j).ge.2) then
                  ind=mod((2*k+1)*(i1+j1),m)
                  term=aco(ind)
                  if(i.eq.1) then
                     term=2d0*term
                  else
                     ind=mod((2*k+1)*iabs((j-i)),m)
                     term=term+aco(ind)
                  endif
               else
                  if(iabs(i-j).eq.1) then
                     ind=mod(2*k+1,m)
                     t1=asi(ind)/coef/deltax+aco(ind)
                     if(i.ne.1) then
                        ind=mod((4*k+2)*i1,m)
                        t2=asi(ind)/coef/deltax
                        if(i.gt.j) then
                           ind=mod((2*k+1)*(2*i1-1),m)
                           term=(t1+t2-asi(ind)/coef/deltax+
f                           aco(ind))/2d0
                        else
                           ind=mod((2*k+1)*(2*i1+1),m)
                           term=(t1-t2+asi(ind)/coef/deltax+
f                           aco(ind))/2d0
                     endif
                  else
                     ind=mod((2*k+1)*(2*i1+1),m)
                     term=(t1-t2+asi(ind)/coef/deltax+
f                           aco(ind))/2d0
                  endif
               endif
            endif
         enddo
      enddo

```

```

                endif
            else
                term=t1
            endif
        else
            ind=mod(2*k+1,m)
            term=asi(ind)/coef/deltax
            ind=mod((4*k+2)*i1,m)
            term=term*(1d0+aco(ind))
        endif
    endif
endif
term=term/gamma
sum=sum+term
c      if(dabs(term/sum).lt.epssum)goto 1200
1100  continue
c      write(iwrite,99999)n,epssum
1200  sum=sum*rnum(n,i)*rnum(n,j)/den(n,i)/den(n,j)
      gr3d=gr3d+sum
      if(n.gt.next.and.dabs(sum/(gr3d+grref)).lt.epsmod)goto 2000
1000  continue
      write(iwrite,99998)maxmod,epsmod,i,j
2000  gr3d=gr3d/r1
      ratio=gr3d*pi/gr
      write(iwrite,99997)ratio,i,j
      return
99999 format(' sum does not converge that rapidly, n=',i12,/
           & ' within tolerance',d20.13)
99998 format(' mode number',i12,' is still significant'/
           & ' within tolerance',d20.13,' for entry',2i12)
99997 format(' ratio of 3d correction on 2d term is',d20.13,/
           & ' for entry',2i12)
cccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
c
c      end of routine sum3d
c
cccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
end

```

□